

## Compilers

## Local Optimization

## Local Optimization

- The simplest form of optimization
- Optimize one basic block
- No need to analyze the whole procedure body


## Local Optimization

- Some statements can be deleted

$$
\begin{aligned}
& x:=x+0 \\
& x:=x * 1
\end{aligned}
$$

- Some statements can be simplified

$$
\begin{array}{ll}
x:=x * 0 & \Rightarrow x:=0 \\
y:=y * * 2 & \Rightarrow y:=y * y \\
x:=x * 8 & \Rightarrow x:=x \ll 3 \\
x:=x * 15 & \Rightarrow t:=x \ll 4 ; x:=t-x
\end{array}
$$

(on some machines << is faster than *; but not on all!)

## Local Optimization

- Operations on constants can be computed at compile time
- If there is a statement $x:=y$ op $z$
- And $y$ and $z$ are constants
- Then y op $z$ can be computed at compile time
- Example: $x:=2+2 \Rightarrow x:=4$
- Example: if $2<0$ jump $L$ can be deleted


## Local Optimization

- Constant folding can be dangerous.


## Local Optimization

- Eliminate unreachable basic blocks:
- Code that is unreachable from the initial block
- E.g., basic blocks that are not the target of any jump or "fall through" from a conditional
- Removing unreachable code makes the program smaller
- And sometimes also faster
- Due to memory cache effects
- Increased spatial locality


## Local Optimization

- Why would unreachable basic blocks occur?


## Local Optimization

- Some optimizations are simplified if each register occurs only once on the left-hand side of an assignment
- Rewrite intermediate code in single assignment form

$$
\begin{aligned}
& x:=z+y \\
& \mathrm{a}:=\mathrm{x} \\
& \mathrm{x}:=2 * \mathrm{x}
\end{aligned} \quad \Rightarrow \quad \begin{aligned}
& \mathrm{b}:=\mathrm{z}+\mathrm{y} \\
& \mathrm{a}:=\mathrm{b} \\
& \mathrm{x}:=2 * \mathrm{~b}
\end{aligned}
$$

( $b$ is a fresh register)

- More complicated in general, due to loops


## Local Optimization

- If
- Basic block is in single assignment form
- A definition $x:=$ is the first use of $x$ in a block
- Then
- When two assignments have the same rhs, they compute the same value
- Example:

(the values of $x, y$, and $z$ do not change in the ... code)


## Local Optimization

- If $w:=x$ appears in a block, replace subsequent uses of $w$ with uses of $x$
- Assumes single assignment form
- Example:

$$
\begin{aligned}
& \mathrm{b}:=\mathrm{z}+\mathrm{y} \\
& \mathrm{a}:=\mathrm{b} \\
& \mathrm{x}:=2 * \mathrm{a}
\end{aligned} \quad \Rightarrow \quad \begin{aligned}
& \mathrm{b}:=\mathrm{z}+\mathrm{y} \\
& \mathrm{a}:=\mathrm{b} \\
& \mathrm{x}:=2 * \mathrm{~b}
\end{aligned}
$$

- Only useful for enabling other optimizations
- Constant folding
- Dead code elimination


## Local Optimization

- Example:

$$
\begin{array}{ll}
\mathrm{a}:=5 \\
\mathrm{x}:=2 * \mathrm{a} \\
\mathrm{y}:=\mathrm{x}+6 \\
\mathrm{t}:=\mathrm{x} * \mathrm{y}
\end{array} \quad \Rightarrow \quad \begin{aligned}
& \mathrm{a}:=5 \\
& \mathrm{x}:=10 \\
& \mathrm{y}:=16 \\
& \mathrm{t}:=\mathrm{x} \ll 4
\end{aligned}
$$

## Local Optimization

If
w := rhs appears in a basic block
w does not appear anywhere else in the program

## Then

the statement $\mathrm{w}:=$ rhs is dead and can be eliminated

- Dead = does not contribute to the program's result

Example: ( a is not used anywhere else)

$$
\begin{aligned}
& x:=z+y \\
& a:=x \\
& x:=2 * a
\end{aligned} \Rightarrow \begin{gathered}
b:=z+y \\
a:=b \\
x:=2 * b
\end{gathered} \Rightarrow \quad \begin{gathered}
b:=z+y \\
x:=2 * b
\end{gathered}
$$

## Local Optimization

- Each local optimization does little by itself
- Typically optimizations interact
- Performing one optimization enables another
- Optimizing compilers repeat optimizations until no improvement is possible
- The optimizer can also be stopped at any point to limit compilation time


## Local Optimization

- Initial code:

$$
\begin{aligned}
& \mathrm{a}:=\mathrm{x}^{* *} 2 \\
& \mathrm{~b}:=3 \\
& \mathrm{c}:=\mathrm{x} \\
& \mathrm{~d}:=\mathrm{c}^{*} \mathrm{c} \\
& \mathrm{e}:=\mathrm{b} * 2 \\
& \mathrm{f}:=\mathrm{a}+\mathrm{d} \\
& \mathrm{~g}:=\mathrm{e}^{*} \mathrm{f}
\end{aligned}
$$

## Local Optimization

- Algebraic optimization:

$$
\begin{aligned}
& \mathrm{a}:=\mathrm{x} * * 2 \\
& \mathrm{~b}:=3 \\
& \mathrm{c}:=\mathrm{x} \\
& \mathrm{~d}:=\mathrm{c} * \mathrm{c} \\
& \mathrm{e}:=\mathrm{b} * 2 \\
& \mathrm{f}:=\mathrm{a}+\mathrm{d} \\
& \mathrm{~g}:=\mathrm{e}^{*} \mathrm{f}
\end{aligned}
$$

## Local Optimization

- Algebraic optimization:

$$
\begin{aligned}
& \mathrm{a}:=\mathrm{x} * \mathrm{x} \\
& \mathrm{~b}:=3 \\
& \mathrm{c}:=\mathrm{x} \\
& \mathrm{~d}:=\mathrm{c} * \mathrm{c} \\
& \mathrm{e}:=\mathrm{b} \ll 1 \\
& \mathrm{f}:=\mathrm{a}+\mathrm{d} \\
& \mathrm{~g}:=\mathrm{e} * \mathrm{f}
\end{aligned}
$$

## Local Optimization

- Copy propagation:

$$
\begin{aligned}
& \mathrm{a}:=\mathrm{x}^{*} \mathrm{x} \\
& \mathrm{~b}:=3 \\
& \mathrm{c}:=\mathrm{x} \\
& \mathrm{~d}:=\mathrm{c}^{*} \mathrm{c} \\
& \mathrm{e}:=\mathrm{b} \ll 1 \\
& \mathrm{f}:=\mathrm{a}+\mathrm{d} \\
& \mathrm{~g}:=\mathrm{e}^{*} \mathrm{f}
\end{aligned}
$$

## Local Optimization

- Copy propagation:

$$
\begin{aligned}
& \mathrm{a}:=\mathrm{x}^{*} \mathrm{x} \\
& \mathrm{~b}:=3 \\
& \mathrm{c}:=\mathrm{x} \\
& \mathrm{~d}:=\mathrm{x} * \mathrm{x} \\
& \mathrm{e}:=3 \ll 1 \\
& \mathrm{f}:=\mathrm{a}+\mathrm{d} \\
& \mathrm{~g}:=\mathrm{e} * \mathrm{f}
\end{aligned}
$$

## Local Optimization

- Constant folding:

$$
\begin{aligned}
& \mathrm{a}:=x^{*} \mathrm{x} \\
& \mathrm{~b}:=3 \\
& \mathrm{c}:=\mathrm{x} \\
& \mathrm{~d}:=\mathrm{x}^{*} \mathrm{x} \\
& \mathrm{e}:=3 \ll 1 \\
& \mathrm{f}:=\mathrm{a}+\mathrm{d} \\
& \mathrm{~g}:=\mathrm{e}^{*} \mathrm{f}
\end{aligned}
$$

## Local Optimization

- Constant folding:

$$
\begin{aligned}
& \mathrm{a}:=x^{*} \mathrm{x} \\
& \mathrm{~b}:=3 \\
& \mathrm{c}:=\mathrm{x} \\
& \mathrm{~d}:=\mathrm{x}^{*} \mathrm{x} \\
& \mathrm{e}:=6 \\
& \mathrm{f}:=\mathrm{a}+\mathrm{d} \\
& \mathrm{~g}:=\mathrm{e}^{*} \mathrm{f}
\end{aligned}
$$

## Local Optimization

- Common subexpression elimination:

$$
\begin{aligned}
& \mathrm{a}:=x^{*} \mathrm{x} \\
& \mathrm{~b}:=3 \\
& \mathrm{c}:=\mathrm{x} \\
& \mathrm{~d}:=\mathrm{x}^{*} \mathrm{x} \\
& \mathrm{e}:=6 \\
& \mathrm{f}:=\mathrm{a}+\mathrm{d} \\
& \mathrm{~g}:=\mathrm{e}^{*} \mathrm{f}
\end{aligned}
$$

## Local Optimization

- Common subexpression elimination:

$$
\begin{aligned}
& \mathrm{a}:=x^{*} \mathrm{x} \\
& \mathrm{~b}:=3 \\
& \mathrm{c}:=\mathrm{x} \\
& \mathrm{~d}:=\mathrm{a} \\
& \mathrm{e}:=6 \\
& \mathrm{f}:=\mathrm{a}+\mathrm{d} \\
& \mathrm{~g}:=\mathrm{e}^{*} \mathrm{f}
\end{aligned}
$$

## Local Optimization

- Copy propagation:

$$
\begin{aligned}
& a:=x^{*} x \\
& b:=3 \\
& c:=x \\
& d:=a \\
& e:=6 \\
& f:=a+d \\
& g:=e^{*} f
\end{aligned}
$$

## Local Optimization

- Copy propagation:

$$
\begin{aligned}
& a:=x^{*} x \\
& b:=3 \\
& c:=x \\
& d:=a \\
& e:=6 \\
& f:=a+a \\
& g:=6 * f
\end{aligned}
$$

## Local Optimization

- Dead code elimination:

$$
\begin{aligned}
& \mathrm{a}:=x^{*} \mathrm{x} \\
& \mathrm{~b}:=3 \\
& \mathrm{c}:=\mathrm{x} \\
& \mathrm{~d}:=\mathrm{a} \\
& \mathrm{e}:=6 \\
& \mathrm{f}:=\mathrm{a}+\mathrm{a} \\
& \mathrm{~g}:=6^{*} \mathrm{f}
\end{aligned}
$$

## Local Optimization

- Dead code elimination:

$$
\mathrm{a}:=x^{*} \mathrm{x}
$$

$$
\begin{aligned}
& f:=a+a \\
& g:=6^{*} f
\end{aligned}
$$

- This is the final form

Which of the following are valid local optimizations for the given basic block? Assume that only $g$ and $x$ are referenced outside of this basic block.
$\square$ Copy propagation: Line 4 becomes $\mathrm{d}:=\mathrm{a}$ * b .


Common subexpression elimination:
Line 5 becomes e := d.
$\square$ Dead code elimination: Line 3 is removed.


After many rounds of valid optimizations, the entire block can be reduced to $\mathrm{g}:=5$.

## Local Optimization

1 a := 1
2 b:= 3
3 c :=a+x
4 d:=a*3
5 e := b * 3
$6 f:=a+b$
$7 \mathrm{~g}:=\mathrm{e}-\mathrm{f}$

