

# Relational Databases

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Relational Algebra (2)  
Set operators, renaming,  
notation

Relational algebra query (expression) on set of relations produces relation as a result

**College**(cName, state, enrollment)

**Student**(sID, sName, GPA, sizeHS)

**Apply**(sID, cName, major, decision)

College

cName	state	enr

Student

sID	sName	GPA	HS

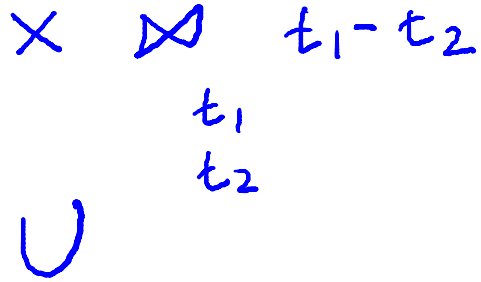
Apply

sID	cName	major	dec

## Union operator

List of college and student names

Stanford  
 Susan  
 Cornell  
 Mary  
 John  
 ⋮



$\pi_{cName} College \cup$   
 $\pi_{sName} Student$

College

cName	state	enr

Student

sID	sName	GPA	HS

Apply

sID	cName	major	dec

## Difference operator

*IDs and names of students who didn't apply anywhere*

$$\left( \left( \pi_{sID} \text{ Student} - \pi_{sID} \text{ Apply} \right) \bowtie \text{ Student} \right)$$

↖  $\pi_{sName}$

college

cName	state	enr

Student

sID	sName	GPA	HS

Apply

sID	cName	major	dec

## Intersection operator

*Names that are both a college name and a student name*

$$\pi_{cName} \text{ College} \cap \pi_{sName} \text{ Student}$$

College

cName	state	enr

Student

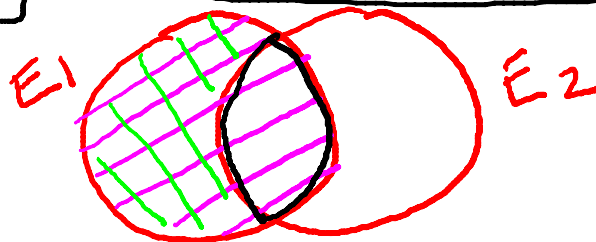
sID	sName	GPA	HS

Apply

sID	cName	major	dec

## Intersection doesn't add expressive power (1)

$$\underline{E_1 \cap E_2} \equiv \underline{E_1 - (E_1 - E_2)}$$



college

cName	state	enr

Student

sID	sName	GPA	HS

Apply

sID	cName	major	dec

## Intersection doesn't add expressive power (2)

$$E_1 \cap E_2 \equiv E_1 \bowtie E_2$$

schema =

College

cName	state	enr

Student

sID	sName	GPA	HS

Apply

sID	cName	major	dec

## Rename operator

1.  $\rho_{R(A_1, \dots, A_n)}(E)$  ← ← General ★
2.  $\rho_R(E)$
3.  $\rho_{A_1, \dots, A_n}(E)$

college

cName	state	enr

student

sID	sName	GPA	HS

Apply

sID	cName	major	dec



## Rename operator

To unify schemas for set operators

*List of college and student names*

$$\rho_{C(\text{name})}(\pi_{\underline{cName}} \text{College}) \cup \rho_{C(\text{name})}(\pi_{\underline{sName}} \text{Student})$$

college

cName	state	enr

student

sID	sName	GPA	HS

Apply

sID	cName	major	dec

## Rename operator

For disambiguation in “self-joins”

*Pairs of colleges in same state*

$$\sigma_{n1 < n2} ( \rho_{c1(n1, s, e1)}(\text{College}) \bowtie \rho_{c2(n2, s, e2)}(\text{college}) )$$

Berkeley Stanford

college

cName	state	enr

Student

sID	sName	GPA	HS

Apply

sID	cName	major	dec

## Alternate notation (1)

Assignment statements – *Pairs of colleges in same state*

$C1 := \rho_{c1, s, e1} \text{ College}$   
 $C2 := \rho_{c2, s, e2} \text{ College}$   
 $CP := C1 \bowtie C2$   
 $Ans := \sigma_{n1 < n2} CP$

College

cName	state	enr

Student

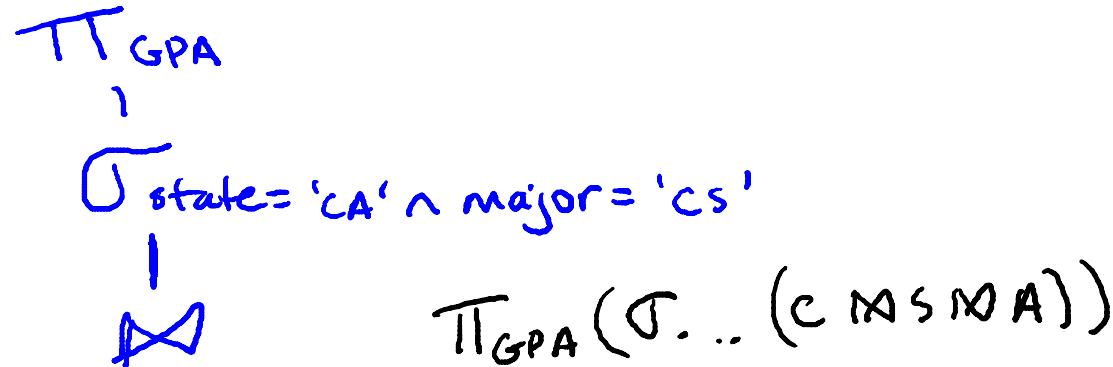
sID	sName	GPA	HS

Apply

sID	cName	major	dec

## Alternate notation (2)

Expression tree – *GPA's of students applying to CS in CA*



College			Student				Apply			
cName	state	enr	sID	sName	GPA	HS	sID	cName	major	dec

## Relational Algebra summary

Core

$R$   
 $\sigma_C(E)$   
 $\pi_{A_1, \dots, A_n}(E)$   
 $(E_1) \times (E_2)$   
 $E_1 \cup E_2$   
 $E_1 - E_2$   
 $\rho_{R(A_1, \dots, A_n)}(E)$

Abbrev.

$\left\{ \begin{array}{l} E_1 \bowtie E_2 \\ E_1 \bowtie_{\theta} E_2 \\ E_1 \cap E_2 \end{array} \right.$

Webcam Video  
(delete this  
in final version!)